

## AC analysis of switched-capacitor networks

### Method: Separate simulation and combination of both switching phases

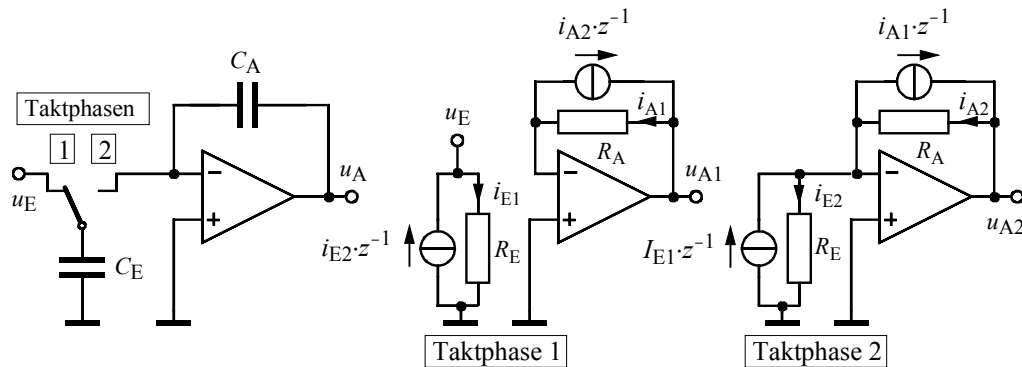
**Principle:** Combination of two separate blocks with cross-coupled controlled current sources.

**Example:** See Fig. 1 (S/C integrator).

Current  $i_{A2}$  (right amplifier) controls the corresponding current source in the left amplifier. Corresponding cross-coupling for the other 3 currents.

Each switched capacitor is replaced by a parallel combination of a current source and a resistor. The resistor value is determined by the sampling frequency and the capacitor value (see example below).

Both output signals  $u_{A1}$  and  $u_{A2}$  are to be added.



**Fig. 1** SC-Integrator (Superposition of both output voltages  $u_{A1}$  and  $u_{A2}$ )

**Example:** Classical *RC-Miller-Integrator*:  $R_1=10\text{ k}\Omega$ ,  $C_2=15,9\text{ nF}$  ( $\tau=159\text{ }\mu\text{s}$ ,  $f_0=1/(2\pi\tau)=1\text{ kHz}$ );

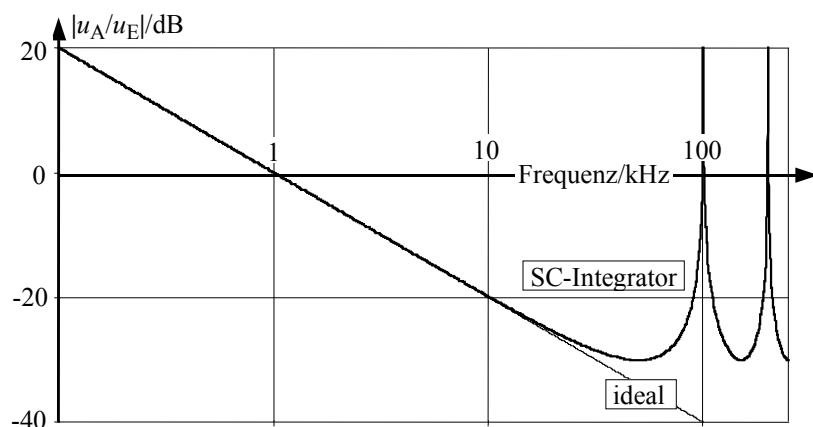
– SC-Äquivalent (Fig. 1, left): Sampling period  $T_A=10\text{ }\mu\text{s}$ ,  $C_E=T_A/R_1=1\text{ nF}$ ,  $C_A=C_2=15,9\text{ nF}$ ;

– For simulation (Fig. 1, right)  $R_E=T_A/C_E=10\text{ k}\Omega$ ,  $R_A=T_A/C_A=628,3\text{ }\Omega$ ,  $z^{-1}=\exp(-j\omega T_A)$ ;

Remark:

Most simulation programs contain controlled sources allowing *Laplace* notation  $s=j\omega$  and  $z^{-1}=\exp(-s\cdot 1E-5)$ . For correct determination of the current direction for all currents  $i_E$  and  $i_A$  it is recommended to use in addition zero-voltage sources in series to  $R_E$  and  $R_A$ , correspondingly.

Perform an ac analysis (input node  $u_E$ ). Both output voltages  $u_{A1}$  and  $u_{A2}$  are added and the transfer function  $u_A/u_E$  can be displayed, as shown in Fig. 2.



**Fig. 2** Transfer function: SC-Structure (Fig. 1), and for comparison: Ideal integration.

Remark: In practice, the output of S/C stages resembles a sample-and-hold function – leading to a drastical improvement of the integrator function for all frequencies above 10 kHz.