Sensitivity and vector margin

With the loop gain function L_0 and the denominator of the closed loop transfer function we can define the "sensitivity figure" S as follows:

$$\begin{split} &\frac{1}{\left|1-\underline{L}_{0}(j\omega)\right|}=\left|\underline{S}(j\omega)\right|<1 \quad \Rightarrow neg.feedback \ ,\\ &\frac{1}{\left|1-\underline{L}_{0}(j\omega)\right|}=\left|\underline{S}(j\omega)\right|>1 \quad \Rightarrow pos.feedback \ . \end{split}$$

Using this definition it is easy to discriminate between pos. and neg. feedback.

Example (see the figure)

Opamp with $A_{0,\text{max}}$ = 100 dB and two poles at 16 Hz and 1,6 MHz and with unity gain feedback.



Transition from negative to positive feedback: f=1,1 MHz.

At 1,8 MHz we have $|S|_{\text{max}} \approx 1,45$ – equivalent to a vector margin of app. $1/1,45 \approx 0,7$.

(The expression $1/|\underline{S}(j\omega)|_{max}$ is identical to the minimum distance between the Nyquist curve $\underline{L}_0(j\omega)$ and the critical point "+1" in the complex plane and is called "vector margin")